

Lab Assignment 6

In this assignment you are to write a program to solve the following problem. As with all lab assignments, remember the following submission steps:

- Make sure your code passes at least all the provided JUnit tests
- Save, commit, and push all code changes
- Confirm the latest code is visible via the "Files" section of your repository website
- Confirm that the repository is private, and that the instructor has Developer access
- Note: you do **NOT** need to document your code

Problem a (LA6a.java)

Write a program to compute the square root of a number. DO NOT USE any math libraries/methods in this program. You will be using the Babylonian method (a.k.a. Heron's method) to approximate the square root¹.

To calculate the square root of x, the Babylonian method requires three inputs: x, an initial guess for the square root, and the error tolerance. It uses a repetitive calculation to get closer and closer to the actual value of the square root: after each iteration, the method checks if the absolute value of the difference between **nextGuess** and **lastGuess** is less than the error tolerance; if so, it stops and returns the value of **nextGuess** as the square root, otherwise if the difference between **nextGuess** and **lastGuess** is larger than the error tolerance, it repeats the calculation. Here is an example (x is 16, the initial guess is 6, and the error tolerance is 0.5):

- The first iteration computes **nextGuess** to be $\frac{6+16/6}{2} = 4.3333$.
- Next, check the difference between the **lastGuess** (6) and **nextGuess** (4.3333). The absolute value of the difference is 1.6667, which is greater than the error tolerance of 0.5. So, repeat the calculation.
- The second iteration computes **nextGuess** to be $\frac{4.3333+16/4.3333}{2} = 4.0128$.
- Check the difference between **lastGuess** (4.3333) and **nextGuess** (4.0128). The absolute value of the difference is 0.3205, which is less than the error tolerance of 0.5. So, the procedure stops and returns 4.0128 as the square root of 16.

Your program needs three methods: **main**, **squareRoot**, and **absoluteValue**. The **main** method should get all three inputs from the user (x, initial guess, and error), run the **squareRoot** method, and output the approximate value of the square root (using exactly five decimal places, rounding if necessary). As always, you must validate the user's inputs – all three must be positive. If the user enters a value that is not positive, then your **main** method should prompt them to enter the value again (and repeat until they enter a valid input).

As you cannot use any math libraries/methods, you will also need to write your own **absoluteValue** method. Only the **main** method should interact with the user (getting inputs and displaying results). The **squareRoot** and **absoluteValue** methods must not contain any input/output statements.

¹ <u>https://en.wikipedia.org/wiki/Methods_of_computing_square_roots - Babylonian_method</u>